## BHARATI VIDYAPEETH'S

## INSTITUTE OF COMPUTER APPLICATIONS \& MANAGEMENT (BVICAM)

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## Assignment - 2

(Based on Unit - III)

| Sr. No. | Question | BTL | CO | Marks |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Assume $G$ is an abelian group with identity e, prove that all elements $x$ of $G$ satisfying the equation $x^{2}=e$ form a subgroup H of G . | BTL4 | CO 2 | 5 |
| 2 | Assume G is the set of all ordered pairs $(\mathrm{a}, \mathrm{b})$ where a ( $!=0$ ) and $b$ are real the binary operation * on $g$ is defined by $(\mathrm{a}, \mathrm{~b})^{*}(\mathrm{c}, \mathrm{~d})=(\mathrm{ac}, \mathrm{bc}+\mathrm{d})$ <br> Show that $\left(\mathrm{G},{ }^{*}\right)$ is a non-abelian group. Show also that the subset H of all those elements of G which are of the form $(1, b)$ is a subgroup of $G$. | BTL4 | CO 2 | 5 |
| 3 | Prove that the set of inverses of the elements of a right coset is a left coset, show that (Ha) ${ }^{-1}=a^{-1} \mathrm{H}^{-1}$. | BTL4 | CO 2 | 5 |
| 4 | If for each $a$ and $b$ is group $G(a b)^{2}=a^{2} b^{2}$. Prove $G$ is abelian. | BTL4 | CO 2 |  |
| 5 | If $H$ is a normal subgroup of $G$ and $K$ is a subgroup of G such that H C K C G. Prove That that H is a normal subgroup of $K$ also. | BTL4 | CO 2 | 5 |
| 6 | Given the Generator Matrix G: <br> 10100100 <br> 10111000 <br> 00101101 <br> Corresponding to encoding function $\mathrm{e}: \mathrm{B}^{3} \rightarrow \mathrm{~B}^{8}$, find parity check matrix and decode following received words 10110101, 10011001,00010100 and 00110011. | BTL1 | CO 2 | 5 |
| 7 | Find integer m and n such that $28844 \mathrm{~m}+15712 \mathrm{n}=4$ | BTL1 | CO 4 | 3 |
| 8 | Make use of fermat's little theorem to compute $3^{302}(\bmod 5)$ | BTL4 | CO4 | 3 |

