

BHARATIVIDYAPEETH'S
INSTITUTEOFCOMPUTERAPPLICATIONS\&MANAGEMENT (BVICAM)
(AffiliatedtoGuruGobindSinghIndraprasthaUniversity,ApprovedbyAICTE,NewDelhi)A-
4,PaschimVihar,RohtakRoad,NewDelhi-110063,Visitusat:http://www.bvicam.in/

## Course Code: MCA-101

## Course Name: Discrete Structures

## Class Test

Each question is of 5 marks

| Q1. | Given a set $S$ containing $n$ elements, formulate a proof to show that the number of <br> proper subsets of $S$ is $2^{\wedge} n-n-1$, where a proper subset excludes the empty set and the <br> set itself. |
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| Q2. | Define a relation $R$ on a set $A$ such that $R$ is both reflexive and symmetric but not <br> transitive. Provide a concrete example to illustrate your definition. |
| Q3. | Given a set $A$ with $n$ elements, consider a relation $R$ on $A$ defined such that $R$ is <br> symmetric and antisymmetric. Analyze whether $R$ can be reflexive, providing reasoning <br> for your answer. |
| Q4. | Suppose you have two equivalence relations, $R 1$ and $R 2$, defined on a set $A$. Evaluate <br> whether the intersection of $R 1$ and $R 2$ is also an equivalence relation. Justify your answer <br> with examples. |
| Q5. | Create a matrix representation for a relation $R$ on a set $A$, where $A=\{a, b, c, d\}$, and $R=$ <br> $\{(a, a),(a, b),(b, c),(c, a)\}$. Then, determine whether the relation $R$ is reflexive, symmetric, <br> antisymmetric, and transitive. |
| Q6. | A committee of $k$ members is to be formed from a group of $n$ people. Evaluate the <br> number of ways to form the committee when: $a)$ Order doesn't matter. b) Order does <br> matter. |
| Q7. | lonsider a set $S$ containing $n$ elements. Analyze the number of ways to partition $S$ into <br> non-empty subsets. |
| Q8. | A committee of $k$ members is to be formed from a group of $n$ people. Evaluate the <br> number of ways to form the committee when: $a)$ Order doesn't matter. b) Order does <br> matter. |
| Q9. | Consider a set $S$ containing $n$ elements. Analyze the number of ways to partition $S$ into <br> non-empty subsets. |
| Q10. | Given a permutation of $n$ distinct objects, determine the number of inversions in the <br> permutation. Evaluate the formula for the number of inversions and provide a proof for <br> its correctness. |

